

4. State the volume of the open box,  $v(x)$ , in terms of  $x$ , in descending order.

$$V(x) = L(w)(H) \quad 4x^3 - 39x^2 + 93.5x$$

$$V(x) = (-2x + 8\frac{1}{2})(-2x + 11)(x)$$

$$V(x) = (4x^2 - 22x + 93.5)(x) \quad \underline{V(x) = 4x^3 - 39x^2 + 93.5x}$$

5. State the inequality if we want the volume of the open box to be at least  $37\frac{1}{2}$  cubic inches.

$$\underline{37\frac{1}{2} \leq 4x^3 - 39x^2 + 93.5x}$$

Solve the inequality by following the next steps.

6. Make the right side of the inequality zero by adding or subtracting the same value on both sides.

$$\underline{4x^3 - 39x^2 + 93.5x - 37\frac{1}{2} \geq 0}$$

7. Multiply both sides of the inequality by the smallest positive number so that all the coefficient of the inequality are integers.

$$\left(\frac{2}{1}\right) 4x^3 - 39x^2 + 93.5x - 37\frac{1}{2} = 0 \left(\frac{2}{1}\right)$$

$$\underline{8x^3 - 78x^2 + 187x - 75 \geq 0}$$

8. Let the left side of the inequality be  $f(x)$ .

$$f(x) = \underline{8x^3 - 78x^2 + 187x - 75}$$

9. Use the Rational Zero Theorem to state all possible rational zeros for  $f(x)$ .

$$P = \pm 1, \pm 3, \pm 5, \pm 15, \pm 25, \pm 75$$

$$Q = \pm 1, \pm 2, \pm 4, \pm 8$$

$$\frac{P}{Q} = \pm 1, \pm 3, \pm 5, \pm 15, \pm 25, \pm 75, \pm \frac{1}{2}, \pm \frac{3}{2}, \pm \frac{5}{2}, \pm \frac{15}{2}, \pm \frac{25}{2}, \pm \frac{75}{2}$$

$$\pm \frac{1}{4}, \pm \frac{3}{4}, \pm \frac{5}{4}, \pm \frac{15}{4}, \pm \frac{25}{4}, \pm \frac{75}{4}, \pm \frac{1}{8}, \pm \frac{3}{8}, \pm \frac{5}{8}, \pm \frac{15}{8}, \pm \frac{25}{8}, \pm \frac{75}{8}$$